การคำนวณขนาดตัวอย่าง สำหรับการวิจัยในมนุษย์

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หัวข้อวันนี้



พื้นฐานของวิจัยและ สถิติที่ใช้สำหรับการ คำนวณขนาดตัวอย่าง

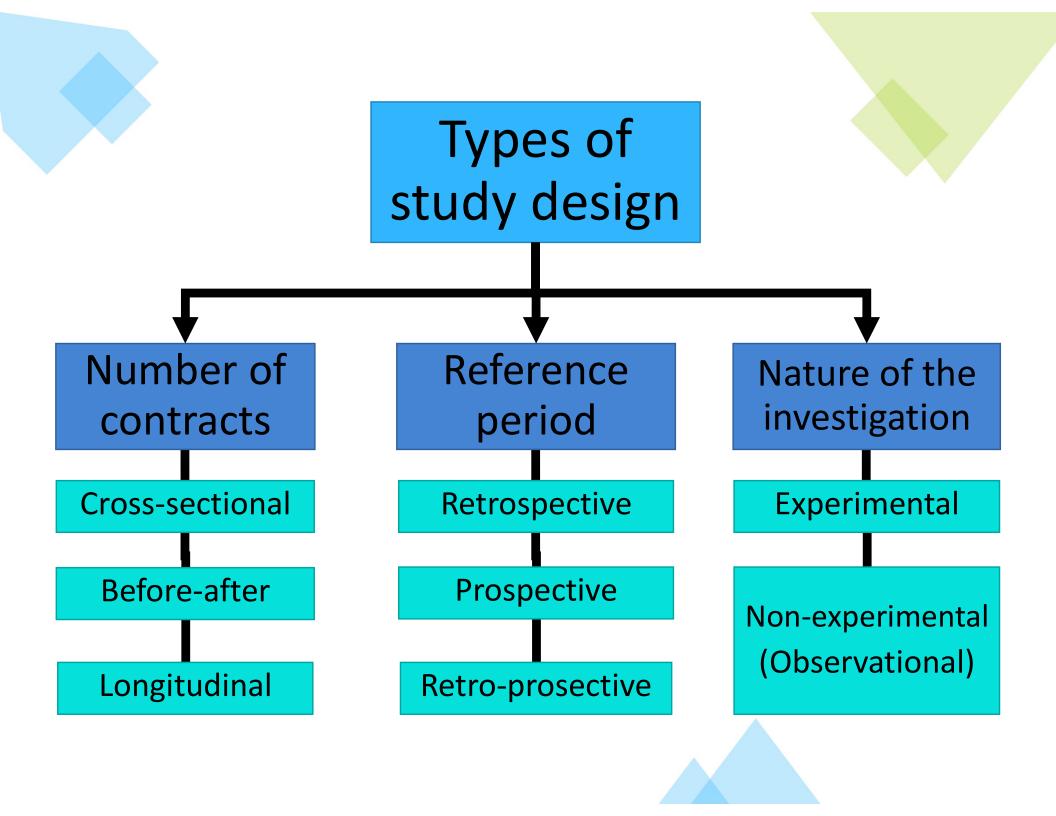


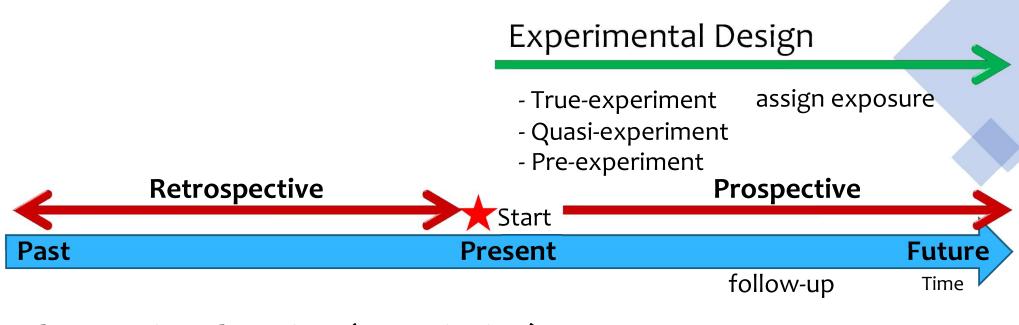
หลักการพิจารณาเลือก
วิธีการคำนวณขนาด
ตัวอย่างที่เหมาะสมกับ
รูปแบบการวิจัย



การใช้โปรแกรมหรือ
แอปพลิเคชั่นสำเร็จรูป
ในการคำนวณขนาด
ตัวอย่าง







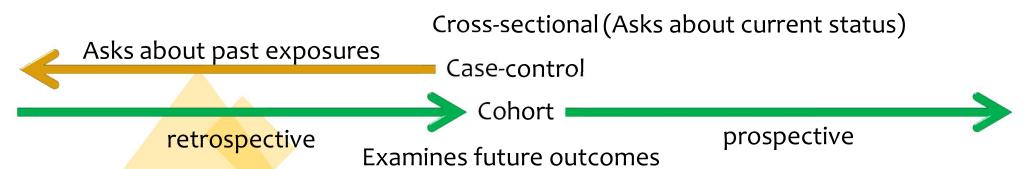
Observational Design (Descriptive)

- Case-report
- Case-series



Trend/Panel

Analytical Design (Cause-and-Effect)



Research Objective

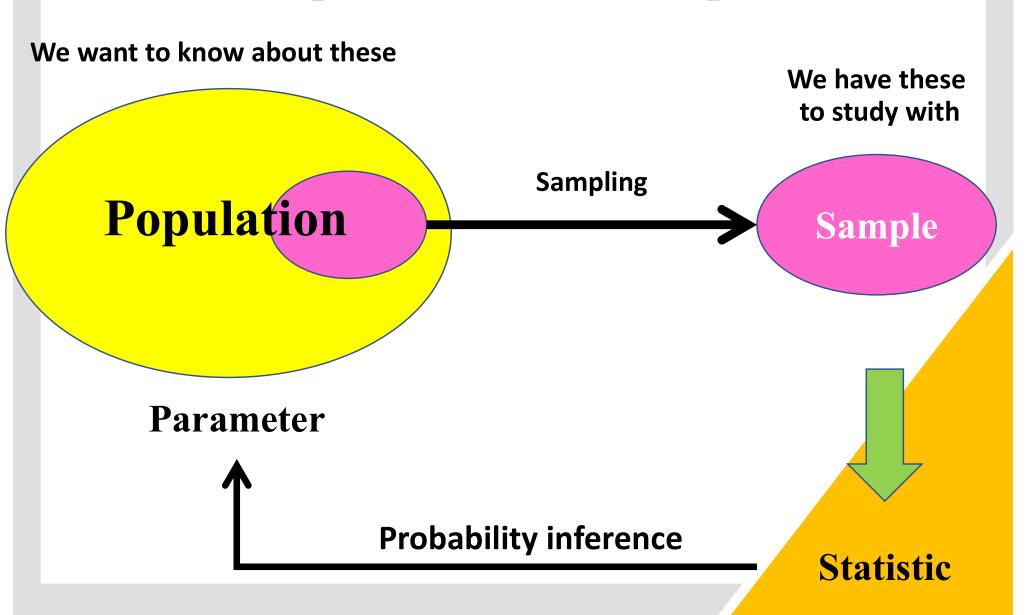
Descriptive

- Design
 - Cross sectional study
 - Sample survey
- Statistical analysis
 - Estimation (no comparison)

Comparison/Association/ Modelling

- Design
 - Analytic study
 - Experimental study
- Statistical analysis
 - Hypothesis testing (comparison)

What is Population and Sample?



- General term: Universe set
- Statistical term:
 All members of a defined group that we are studying or collecting information

Population

Type:

- Finite population
 - Small
 - Large
- Infinite population

Population

Target population

Source population

Eligible population

Sample

Sampling frame (N)

Sample

- Subset of population
- To represent the population well:
 - randomly collected
 - adequately size
- subject => smallest sampling unit

Type of variable

•Independent variable/
Factor/ Treatment/
Predictive

(I)

Dependent variable/Outcome

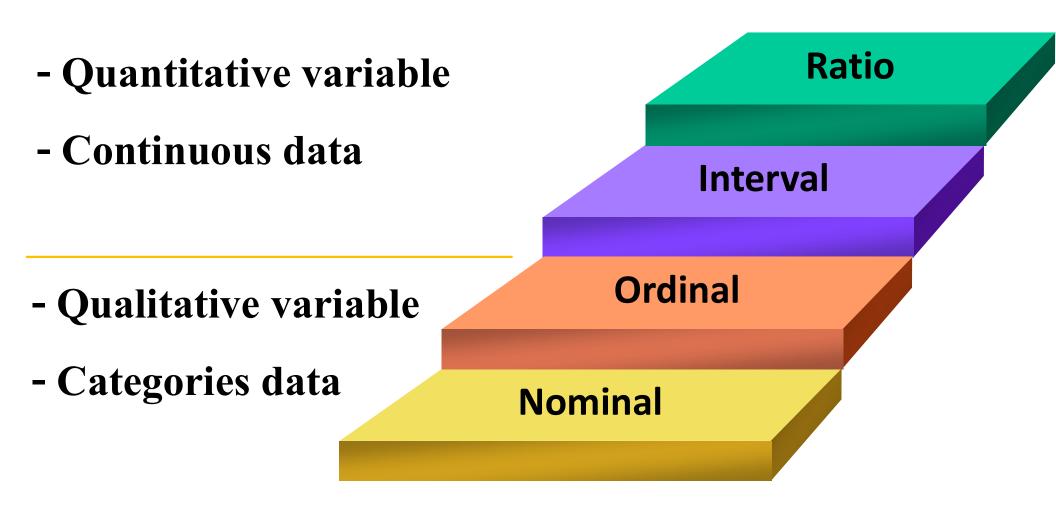
Type of variable

(II)

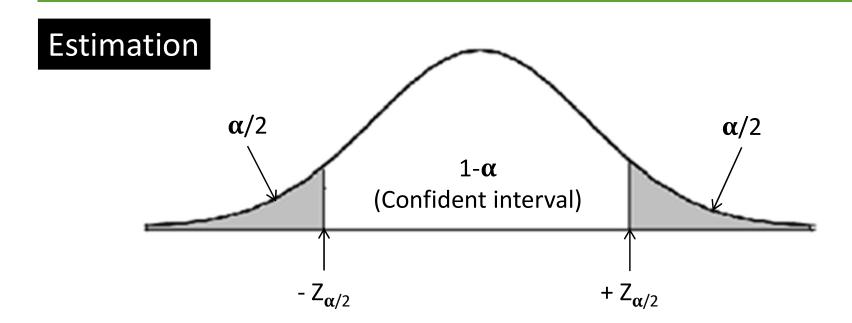
- Quantitative variable
 - Discrete variable
 - Continuous variable

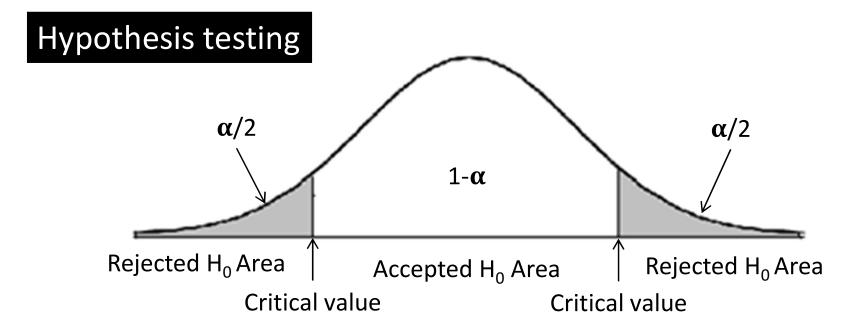
- Qualitative variable
 - Binary/dichotomous variable
 - Polychotomous variable

Measurement levels



Inferential Statistics





Statistical Hypothesis

Two-tail (two-side)

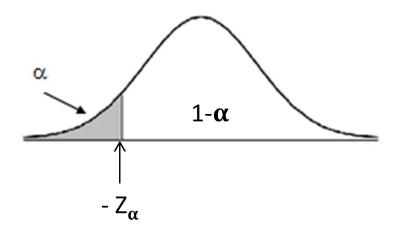
$$H_0$$
: $\mu = \mu_0$

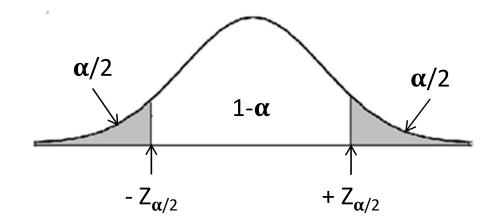
$$H_A$$
: $\mu \neq \mu_0$

One-tail (one-side)

$$H_0: \mu \geq \mu_0$$

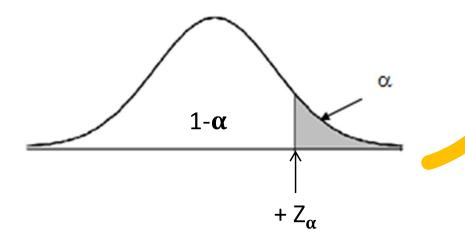
$$H_A$$
: $\mu < \mu_0$





$$H_0: \mu \leq \mu_0$$

$$H_A$$
: $\mu > \mu_0$



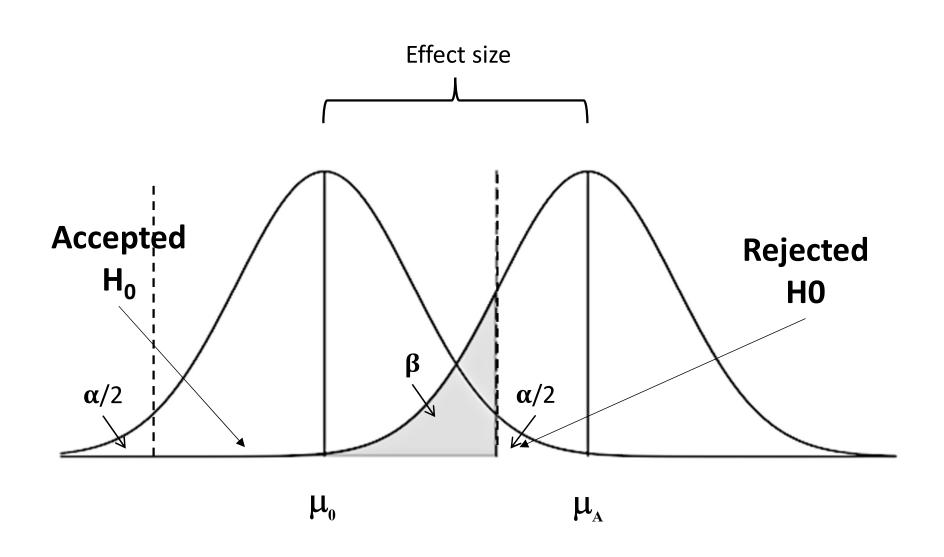
Significance and power

Truth (real world)

Decision
(statistical
analysis)

	No difference	Difference
Accepted H ₀	Correct decision (CI) = 1- α	Type II error = β
Reject H ₀	Type I error level (α =>significance)	Correct decision (power) = 1-β

Significance and power



Z-value by significant level (α)

α	$Z_{\alpha/2}$	Z_{α}
0.10	1.645	1.282
0.05	1.96	1.645
0.01	2.576	2.326

Z-value by Power of test $(1-\beta)$

Power	β	Z_{eta}
80%	0.20	0.842
90%	0.10	1.282
95%	0.05	1.645

How to select sample size equation

Appropriated sample size

- Primary objective
 - for estimation
 - for hypothesis testing: comparison, association
- Primary outcome/parameter
 - => Total, <u>Average</u>, <u>Proportion</u>, Ratio
- Research design
- Sampling technique

Sample size equation (general)

Representative sample in infinite/large populations (Cochran, 1963)

$$n_0 = \frac{Z_{\alpha/2}^2(\text{VARIANCE})}{d^2}$$

When n_0 : number of sample and d = e

d: precision of estimation

e: acceptable sampling error

Sample size equation (general)

Finite population correction

$$n = \frac{n_0}{1 + (\frac{n_0}{N})}$$

When N: number of population

n₀: initial sample size

n : adjusted sample size

Sample size equation for estimation

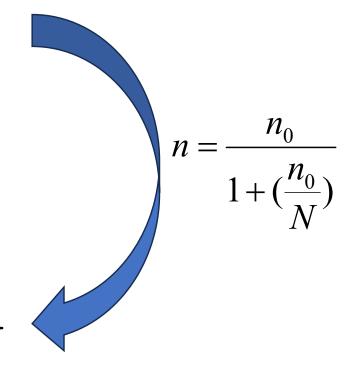
Mean estimation

Infinite population

$$n_0 = \frac{Z_{\alpha/2}^2 \sigma^2}{d^2}$$

Finite population

$$n = \frac{Z_{\alpha/2}^{2} N \sigma^{2}}{Z_{\alpha/2}^{2} \sigma^{2} + (N-1)d^{2}}$$



Sample size equation for estimation

When

- n = number of sample
- N = number of population
- σ = standard deviation of population parameter (estimated by s.d.)
- d = precision of estimation

$$= |\bar{x} - \mu|$$

= $\epsilon^* \mu$ when ϵ = relative precision of estimation = $|\bar{x} - \mu|/\mu$

Example

ในการศึกษาน้ำหนักของทารกแรกคลอดที่เข้าโปรแกรมรับฝากครรภ์ของโรงพยาบาลแห่งหนึ่ง ซึ่งมีสถิติน้ำหนัก ของทารกแรกคลอดทั้งประเทศ มีค่าเฉลี่ย 2800 กรัม s.d. 500 กรัม หากต้องการประมาณค่าเฉลี่ยของน้ำหนัก ทารกแรกคลอดของโรงพยาบาลแห่งนี้ จะต้องเลือกตัวอย่างมาจำนวนเท่าใด

- ตัวแปรที่ศึกษา => น้ำหนักทารกแรกคลอด => เชิงปริมาณ
- วัตถุประสงค์ => ประมาณค่าเฉลี่ย
- สูตรคำนวณขนาดตัวอย่าง => mean estimation
- ผู้ศึกษากำหนด ช่วงความเชื่อมั่น 95% (α=0.05)
 ความคลาดเคลื่อนสัมพัทธ์ไม่เกิน 5% (ε=0.05)
- เมื่อกำหนด $\alpha = 0.05 => Z_{\alpha/2} = 1.96$
- $d = \text{mean*} \mathbf{\mathcal{E}} = 2800*0.05 = 140$
- σ = s.d. = 500
- แทนค่า

$$n_0 = \frac{Z_{\alpha/2}^2 \sigma^2}{d^2} = \frac{1.96^2 \times 500^2}{140^2} = 49$$

ดังนั้นจะต้องสุ่มทารกแรกคลอดมาจำนวน 49 คน

Sample size equation for estimation

Proportion estimation

Infinite population

$$n_0 = \frac{Z_{\alpha/2}^2 \pi (1 - \pi)}{d^2}$$

Finite population

$$n = \frac{Z_{\alpha/2}^{2} N \pi (1 - \pi)}{Z_{\alpha/2}^{2} \pi (1 - \pi) + (N - 1)d^{2}}$$

$$n = \frac{n_0}{1 + (\frac{n_0}{N})}$$

Sample size equation for estimation

When

- •n = number of sample
- N = number of population
- π = proportion of population parameter
- d = precision of estimation

$$= |p - \pi|$$

Example

ในการศึกษาภาวะกระดูกพรุนในประชากรวัยกลางคนของโรงพยาบาลแห่งหนึ่ง ซึ่งจากการศึกษาของ Lekamwasam (2009) ที่พบภาวะกระดูกพรุนในอาสาสมัคร 5.8% (p=0.058) ดังนั้นจะต้องเลือกตัวอย่างมาจำนวนเท่าใด

- ตัวแปรที่ศึกษา => ภาวะกระดูกพรุน => เชิงคุณภาพ (สัดส่วนของภาวะกระดูกพรุน)
- วัตถุประสงค์ => ประมาณค่าสัดส่วน
- สูตรคำนวณขนาดตัวอย่าง => proportion estimation
- ผู้ศึกษากำหนด ช่วงความเชื่อมั่น 95% (α=0.05)
 ความคลาดเคลื่อนที่ยอมให้เกิดขึ้นได้ไม่เกิน 5% (e=0.05)
- เมื่อกำหนด $\alpha = 0.05 => Z_{\alpha/2} = 1.96$
- แทนค่า

$$n_0 = \frac{Z_{\alpha/2}^2 \pi (1 - \pi)}{d^2} = \frac{1.96^2 \times 0.058(1 - 0.058)}{0.05^2} = 83.96$$

ดังนั้นจะต้องสุ่มผู้ชายวัยกลางคนมาจำนวน 84 คน

Sample size equation for estimation

A simplified formula for proportions

Taro Yamane (1967)

$$n = \frac{N}{1 + Ne^2}$$

Define:
$$Z_{\alpha/2}^2 = 2$$

$$\pi = 0.5$$

$$n = \frac{Z_{\alpha/2}^2 N \pi (1 - \pi)}{Z_{\alpha/2}^2 \pi (1 - \pi) + (N - 1)d^2}$$

Yamane, T. (1967). Statistics, An Introductory Analysis, 2nd Ed., New York: Harper and Row.

Sample size equation for estimation

A simplified formula for proportions

Krejcie & Morgan (1970)

$$n = \frac{\chi_{\alpha}^{2} N \pi (1 - \pi)}{\chi_{\alpha}^{2} \pi (1 - \pi) + (N - 1)d^{2}}$$

Define:
$$\chi^2_{\alpha} = \chi^2_{.05,1} = 3.841$$

 $\pi = 0.5$
 $d = 0.05$

Krejcie, RV, & DW Morgan. (1970). Determining Sample Size for Research Activities. *Educational* and Psychological Measurement.

mean difference of one group

Hypothesis

$$H_0 : \mu = \mu_0$$

$$H_A: \mu \neq \mu_0$$

$$H_0: \mu \leq \mu_0$$
 หรือ $H_0: \mu \geq \mu_0$

$$H_A: \mu > \mu_0$$
 $H_A: \mu < \mu_0$

$$n = \frac{(Z_{\alpha/2} + Z_{\beta})^{2} \sigma^{2}}{(\mu - \mu_{0})^{2}}$$

$$n = \frac{\left(Z_{\alpha} + Z_{\beta}\right)^2 \sigma^2}{(\mu - \mu_0)^2}$$

mean difference between 2 independent groups

Hypothesis

$$H_0: \mu_1 = \mu_2$$

$$H_A: \mu_1 \neq \mu_2$$

General

$$n_{\text{per group}} = \frac{(Z_{\alpha/2} + Z_{\beta})^{2} (\sigma_{1}^{2} + \sigma_{2}^{2})}{(\mu_{1} - \mu_{2})^{2}}$$

Define:

$$\sigma_1^2 = \sigma_2^2 = \sigma^2$$

$$n_{\text{per group}} = \frac{(Z_{\alpha/2} + Z_{\beta})^2 2\sigma^2}{(\mu_1 - \mu_2)^2}$$

Define:

$$n = n_1 + n_2$$

$$n = \frac{(Z_{\alpha/2} + Z_{\beta})^2 4\sigma^2}{(\mu_1 - \mu_2)^2}$$

mean difference between 2 dependent groups Hypothesis

$$H_0: \mu_D = 0$$

$$H_A: \mu_D \neq 0$$

$$n = \frac{\left(Z_{\alpha/2} + Z_{\beta}\right)^2 \sigma_D^2}{\mu_D^2}$$

proportion difference between 2 groups

Hypothesis

$$H_0: \pi_1 = \pi_2$$

$$H_A: \pi_1 \neq \pi_2$$

กรณี
$$n_1:n_2=1:1$$

$$n_{\text{per group}} = \frac{\left(Z_{\alpha/2}\sqrt{2\bar{\pi}(1-\bar{\pi})} + Z_{\beta}\sqrt{\pi_1(1-\pi_1) + \pi_2(1-\pi_2)}\right)^2}{(\pi_1 - \pi_2)^2}$$

กรณี
$$n_1:n_2=1:k$$

$$n_{\text{per group}} = \frac{\left(Z_{\alpha/2}\sqrt{(k+1)\bar{\pi}(1-\bar{\pi})} + Z_{\beta}\sqrt{k\pi_1(1-\pi_1) + \pi_2(1-\pi_2)}\right)^2}{(\pi_1 - \pi_2)^2}$$

correlation between 2 continuous variables

Hypothesis

$$H_0: \rho = o$$

$$H_{\Delta}: \rho \neq 0$$

$$n = \frac{\left(Z_{\alpha/2} + Z_{\beta}\right)^{2}}{C(r)} + 3$$

$$C(r) = \frac{1}{2} \ln \left(\frac{1+r}{1-r} \right)$$

Effect size

Cohen's d

$$d = \frac{\bar{x}_1 - \bar{x}_2}{S}$$

$$s_{pooled} = \sqrt{\frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{(n_1 + n_2 - 2)}}$$

Effect size

d = 0.02 : small

d = 0.05: medium

d = 0.80 : large

Cohen, J. (1988). Statistical Power Analysis for the Behavioral Sciences. Routledge.

Sample size equation for hypothesis testing

Effect size (Cohen's d) one group difference

$$n = \frac{\left(Z_{\alpha/2} + Z_{\beta}\right)^2}{\delta^2}$$
 when δ : effect size (d)

two independent group difference

$$n = \frac{2(Z_{\alpha/2} + Z_{\beta})^2}{\delta^2}$$

Sample size equation for Regression

Linear regression

$$n = \left[rac{(Z_{lpha/2} + Z_{eta})\sigma}{\lambda_1 \sigma_x}
ight]^2$$
 when $\sigma = \sqrt{\sigma_y^2 - \lambda_1^2 \sigma_x^2}$ $ho = rac{\sigma_x \lambda_1}{\sigma_y}$

 λ : beta cofficience

$$n_{adj} = \frac{n}{(1 - R^2)}$$

Dupont, W.D. and Plummer, W.D. Power and Sample Size Calculations for Studies Involving Linear Regression. New York, 1998. Print.

Sample size equation for Regression

Logistic regression

$$n = \frac{4\pi(1-P)(Z_{\alpha/2} + Z_{\beta})^2}{(\pi_1 - \pi_2)^2}$$

$$n_{adj} = \frac{n}{(1 - R^2)}$$

when R²: Psudo R²

when using OR $\pi_2 = \frac{OR \times \pi_1}{(1-\pi_1) + OR \times \pi_1}$

Hsieh FY, Bloch DA, Larsen MD. (1998). A simple method of sample size calculation for linear and logistic regression. Statistics in Medicine. 17(14): 1623-34.

Sample size adjustment

Fixed percentage

$$n_{adj.} = n \times \left(1 + \frac{\%}{100}\right)$$

Dropout rate

$$n_{adj.} = n \div \left(1 - \frac{\%dropout}{100}\right)$$



for regression

$$n = 50 + 8 \times \#cofficients$$

Parameter in equation

Consider from:

- 1st outcome
- important variable
- higher variance

Find parameter from:

- Previous research
- Database register
- Pilot study

X

Hand exercise for women with rheumatoid arthritis and decreased hand function: an exploratory randomized controlled trial

https://www.ncbi.nlm.nih.gov

Alt PDF Hand exercise for women with rheumatoid arthritis and decreased hand function: an exploratory randomized controlled trial Arthritis Res Ther. 2019; 21: 158.



joint protection, assistive devices, and alternative ways of performing AD. The hand-exercise program addressed range of motion and muscle strength.

Primary outcome was change in observed ADL motor ability measured by the Assessment of Motor and Process Skills (AMPS).

Baseline measures were repeated after 8 weeks.

of anountation => one-group Experiment

pre-post test mrohenou sample size

(Zon+ ZB) 2 62

Results

Improvements in ADL motor ability in CIP_{EXERCISE} (mean change

= 0.24 logits 95% CI = 0.09 to 0.39 and CIP_{CONTROL} (mean

change =0.20 logits; 95% CI = 0.05 to 0.35) were statistically

significant, with no differences between groups (mean difference =

0.04 logits; 95% CI = -0.16 to 0.25). Thirteen (46.4%) participants

in the CIP_{EXERCISE} and 12 (44.4%) in the CIP_{CONTROL} obtained

clinically relevant improvements (≥ 0.30 logits) in ADL motor ability; this group difference was not significant (z = 0.15; p = 0.88).

gud = pre-post

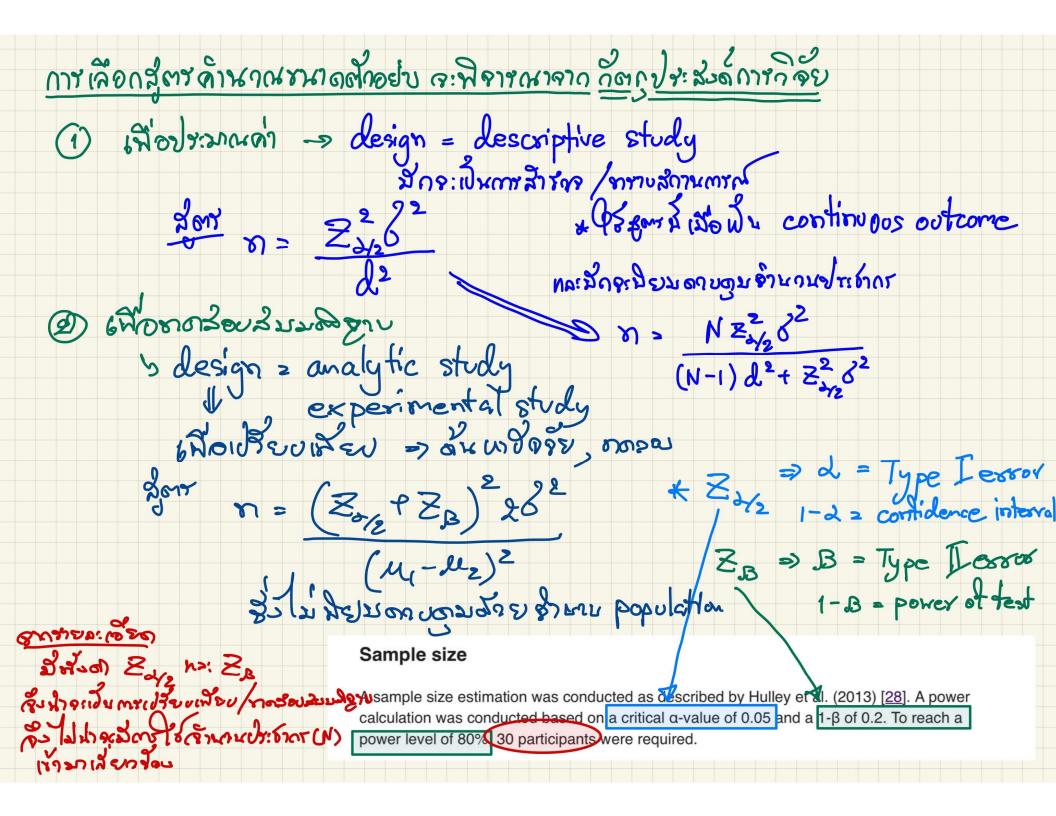
$$= \left(\frac{U_L - d}{b_{LL} \cdot d}\right) \sqrt{\frac{1}{2}}$$

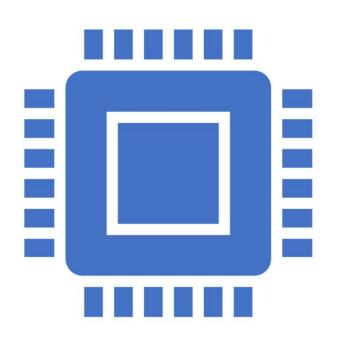
d = 0.05

$$= (0.39 - 0.24) \sqrt{27}$$
2.055

$$n = \frac{(1.96 \pm 0.84)^2 (0.379)^2}{(0.29)^2} = 22011$$

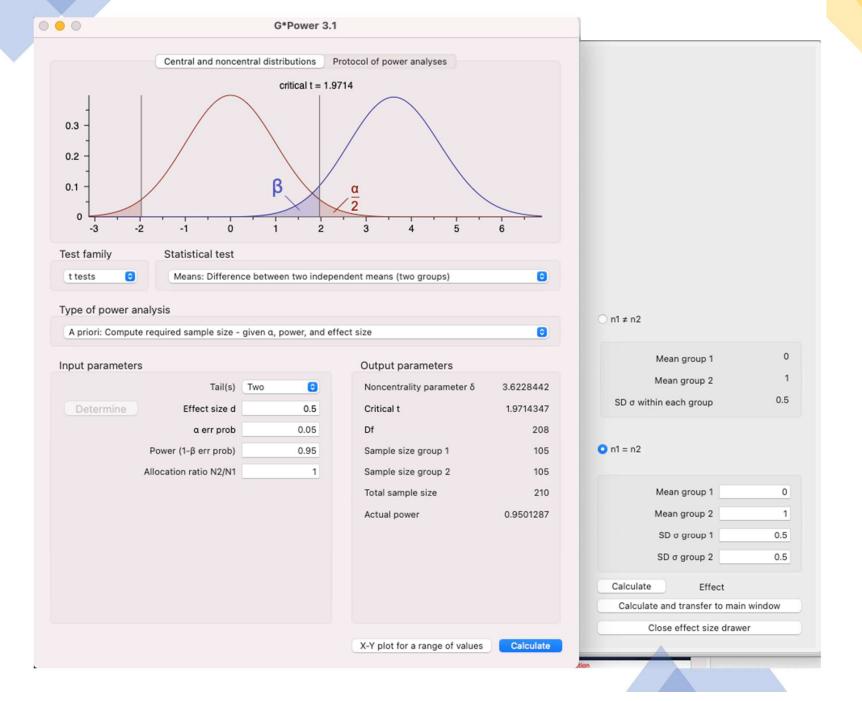
$$n = \frac{(1.96 + 1.29)^2 (0.397)^2}{(0.24)^2}$$



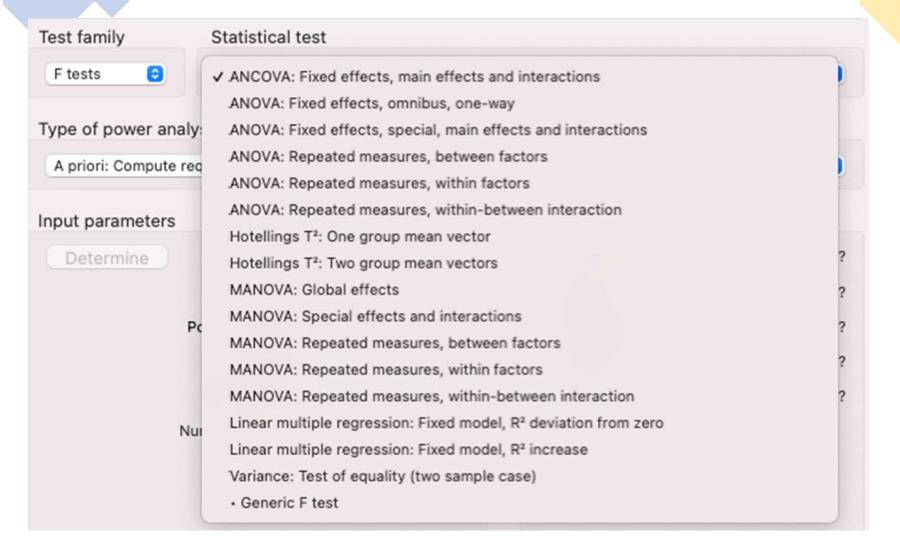


Software & Application

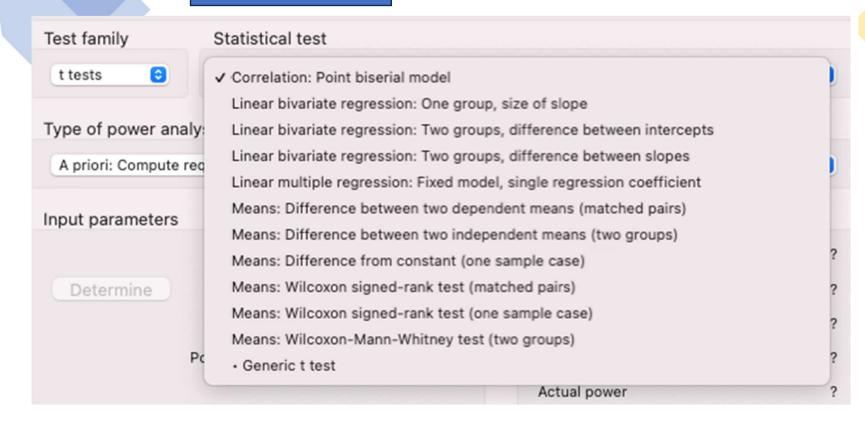
G*Power

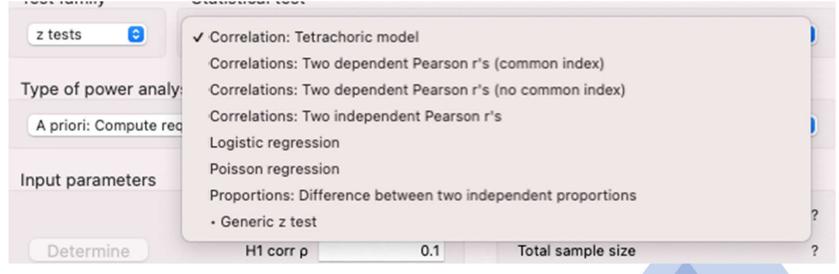


G*Power



G*Power





Web application

https://www.ai-therapy.com/psychology-statistics/sample-size-calculator

Al-Therapy Statistics BETA

Al-Therapy Home

Blog

Help and contact

HYPOTHESIS TESTING

Overview and terminology

Comparing two sets of data

Comparing more than two sets of data (ANOVA)

EFFECT SIZES AND POWER

Effect size calculator

Power calculator

Sample size calculator

PLOTTING

ROC Curve

About Al-Therapy

Al-Therapy creates online fully automated programs using the latest evidence-based treatments, such as cognitive behavioural therapy. The social anxiety program has been tested with a randomized controlled trial. To find out more visit:

- Overcome Social Anxiety
- Overcome Fertility Stress
- Overcome Death Anxiety

A second approach is to use clinical judgment to specify the smallest effect size that you consider to be relevant. For example, if you feel that it is important to detect even small effects, you may select a value of 0.2 (see this page for a rough categorization of effect size levels).

Sample size calculator

This calculator tells you the minimum number of participants necessary to achieve a given power. The following parameters must be set:

Test family The online calculator currently supports the t-test and sample size estimation for

correlation co-efficients. Please contact us if there are other test families that you would

like included.

Sample groups Select the "Same subjects" option if you will take multiple measurements from the same

person (this is sometimes known as "paired", "related" or "repeated measures"), and

"Independent groups" if the scores will be from two different groups of people.

Tail(s) The number of tails depends on whether or not your hypothesis has an implied direction.

There is more information on directionality here.

Effect size See the discussion above to select an appropriate effect size.

Significance level Alpha (α) is the probability of falsely rejecting the null hypothesis, and the most common

value is 0.05. A more thorough discussion on setting the significance level can be found

here.

Power Statistical power is the ability of study to detect a result that is exists in nature. Generally, we want power to be as high as possible. However, setting it too high may result in a

sample size that is not practical. A value of 0.8 is often used in practice.

Test family	t-test	;
Sample groups	Independent groups	;
Number of tails	Two	;
Effect size	0.5	
Significance level (α)	0.05	
Power	0.8	
	0.1 1	

Web application

https://sample-size.net/sample-size-means/





Explore the *Training in*Clinical Research Program
at UCSF

Home

Calculators

CI for proportion

CI for mean

Means - effect size

Means - sample size

Proportions - effect size

Proportions - sample size

CI for proportion - sample size

Survival analysis - sample size

Prevalence

CI for risk ratio

More calculators...

Calculator finder

About calculating sample size

About us

Sample size - Means

Compare the mean of a continuous measurement in two samples. The sample sizes are calculated in two different ways: first using the T statistic (with a non-centrality parameter), then using the Z statistic. The Z statistic approximates the T statistic, but provides sample sizes that are slightly too small. (We provide the Z statistic calculation to allow comparison with other calculators which use the Z approximation.)

Instructions: Enter parameters in the **green** cells. Answers will appear in the blue box below.

α (two-tailed) =	0.05	Threshold probability for rejecting the null hypothesis. Type I error rate.
β =	0.2	Probability of failing to reject the null hypothesis under the alternative hypothesis. Type II error rate.
q ₁ =	0.5	Proportion of subjects that are in Group 1 (exposed)
q ₀ =	0.5	Proportion of subjects that are in Group 0 (unexposed); 1-q $_{1}$
E =	0.5	Effect size (If μ_1 = mean in Group 1 and μ_0 = mean in Group 0, then E = μ_1 - μ_0 .)
S =	1	Standard deviation of the outcome in the population

Calculate

Web application

https://www.danielsoper.com/statcalc/calculator.aspx?id=89

A-priori Sample Size Calculator for Structural Equation Models

This calculator will compute the sample size required for a study that uses a structural equation model (SEM), given the number of observed and latent variables in the model, the anticipated effect size, and the desired probability and statistical power levels. The calculator will return both the minimum sample size required to detect the specified effect, and the minimum sample size required given the structural complexity of the model.

Please enter the necessary parameter values, and then click 'Calculate'.

Anticipated effect size:	0.1	0		
Desired statistical power level:	0.8	0		
Number of latent variables:	2	0		
Number of observed variables:	10	0		
Probability level:	0.05	0		
	Calculate	ell		
► Related Resources				
x² Formulas 💆 Reference	ces 💳 F	Related Calculators	Q Search	



https://www.statulator.com/SampleSize/ss1P.html

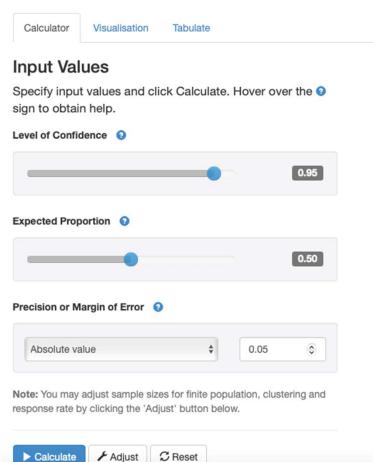
Visualisation

Calculator



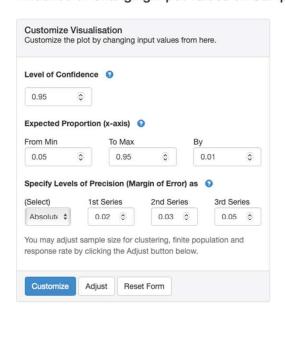
Sample Size Calculator for Estimating a Single Proportion

- Provides live interpretations.
- Assesses the influence of changing input values.
- Adjusts sample sizes for finite population and clustering.



Influence of Changing Input values on Sample Size Estimates

Visualisation



2500				COCCOCC	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	2000000		0% absolute	
			0000	SCI.		-46	5 .	0% absolute	e precis
2000		d	pode				agg	8	
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Mobile application



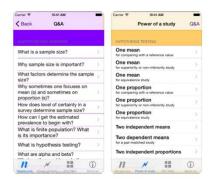






Font preview tool.

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Sample Size Calcula...

Education ★☆☆☆☆ 1 ₿35.00

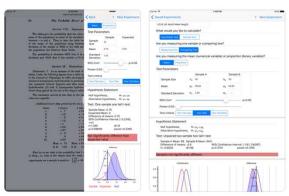


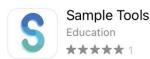


Power Analysis

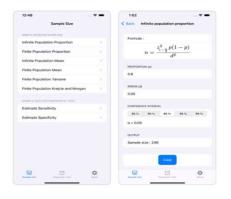
Easy guided statistical tests

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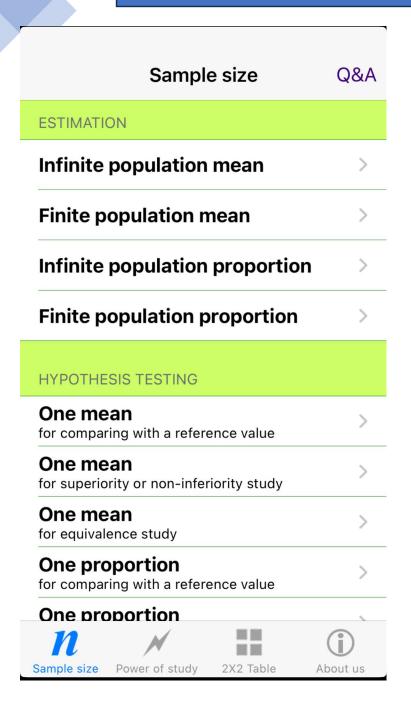


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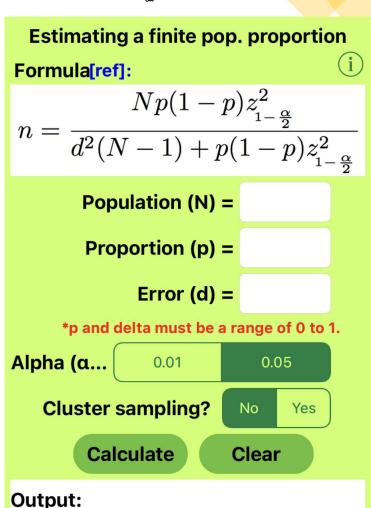


Mobile application



N4studies

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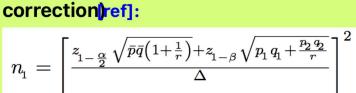


Mobile application

One mean for comparing with a reference value	>
One mean for superiority or non-inferiority study	>
One mean for equivalence study	>
One proportion for comparing with a reference value	>
One proportion for superiority or non-inferiority study	>
One proportion for equivalence study	>
Two independent means	>
Two dependent means for a pair-matched study	>
Two independent proportions	>
Two dependent proportions	

Two independent proportions

Formula (without continuity correction)ref]:



$$r=rac{n_2}{n_1},q_1=1-p_1,q_2=1-p_2$$

$$\bar{p} = \frac{p_1 + p_2 r}{1 + r}, \bar{q} = 1 - \bar{p}$$

Proportion in group1 (p1...

Proportion in group2 (p...

*p₁ and p₂ must be a range of 0 to 1.

Ratio
$$(r) = 1$$

Beta (
$$\beta$$
) = 0.1 0.2

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